

* START LOOKING OVER YOUR TEST

* Get out Extra Credit to turn in

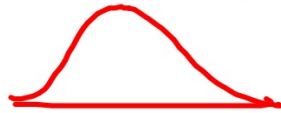
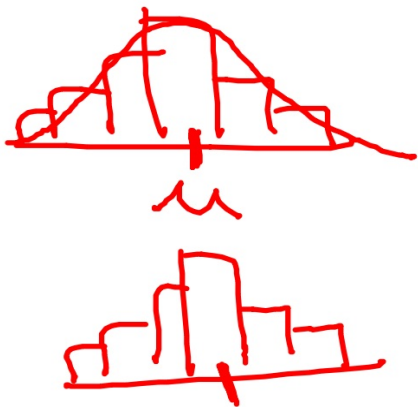
Activity from Friday... what did we learn?

$n=5$ vs. $n=20$

• larger $n \Rightarrow$ smaller standard deviation

\Rightarrow more accurate center

\Rightarrow more normal



WARM UP:

The weights of Labradors follow a normal model with a mean of 42 lbs. and std. dev of 3.4 lbs.

1. Draw the normal model using the 68-95-99.7% rule.
2. What is the probability that you have a dog that weights more than 50 lbs? $P(X > 50)$
3. What is the probability that you have a dog that weights less than 53 lbs? $P(X < 53)$
4. What is the probability that you have a dog that weighs between 41 and 48 lbs? $P(41 < X < 48)$

Ch. 18: Central Limit Theorem

Sampling Distribution-

- * A histogram of repeated samplings
- * We can make histograms of means or of proportions
- * Examples: <sup>$n=5$
 $n=20$</sup> ~~true~~ % males taking the SATs
~~% of foam pieces in bag~~
^{true} avg. score on SATs
- * We use these histograms to help us find the TRUE mean or proportion

CENTRAL LIMIT THEOREM:

- * A sampling distribution can be approximated by a Normal model
- * The larger the sample, the better the approximation will be
- * Does not matter what shape the population is... if the sample size is large enough, the sampling distribution will be Normally shaped

$$np \geq 10$$
$$nq \geq 10$$

Ex: binomial

\bar{X} \hat{p}

PROPORTIONS:

A sample of size n is taken from a population with center p .

\hat{p} = sample prop.

Sampling distribution of sample proportions (\hat{p}):

Mean: $\underline{\mu_{\hat{p}} = p}$ Std. Dev: $\sigma_{\hat{p}} = \sqrt{\frac{pq}{n}}$

The distribution is: $N \left(p, \sqrt{\frac{pq}{n}} \right)$

* According to the CLT, the sample size must be large enough for the sampling distribution to be approx. normal. The following conditions must be met:

1) Simple Random Sample (SRS)

2) np and $nq \geq 10$

3) population $\geq 10n$ independence (10%) rule

Example:

According to the manufacturer of the candy Skittles, 20% of the candy produced is the color red. What is the probability that given a large bag of skittles with 58 candies that we get at least 17 red?

Check

$$N(0.20, \sqrt{\frac{(0.2)(0.8)}{58}})$$

① SRS assumed

$$\textcircled{2} \begin{matrix} np & \geq 10 & 58(0.2) \\ nq & \geq 10 & 58(0.8) \end{matrix} \neq 10$$

③ pop ≥ 10 n skittles $\neq 580$

Normal model

$$P(\hat{p} > \frac{17}{58}) = 0.0381$$

MEANS:

A sample of size n is taken from a population with center μ and std. dev. of σ

Sampling distribution of sample means (\bar{X}):

Mean: $\mu_{\bar{X}} = \mu$ Std. Dev: $\sigma_{\bar{X}} = \frac{\sigma}{\sqrt{n}}$

The distribution is: $N\left(\mu, \frac{\sigma}{\sqrt{n}}\right)$

* According to the CLT, the sample size must be large enough for the sampling distribution to be approx. normal. The following conditions must be met:

1) Simple Random Sample (SRS)

2) $n \geq 30$ or the **population** must be normally distributed

3) population $\geq 10n$

Example:

* Suppose that male seniors have a mean score of μ 1200 with a standard deviation of 130. We take a random sample of 100 male seniors.

① SRS stated

② $n \geq 30$ $100 \neq 30$

(a) What would the distribution of sample means look like?

③ pop $\geq 10n$ male seniors $\neq 1000$

$$N(1200, \frac{130}{\sqrt{100}})$$

(b) What would be the probability that we would get an average of less than 1150?

$$P(\bar{X} < 1150) = 6 \times 10^{-5}$$

p. 434

#15

#37

HW answers:

①5 $p = 0.07$
 $n = 200$

a) $\mu_{\hat{p}} = p = 0.07$

$$\sigma_{\hat{p}} = \sqrt{\frac{pq}{n}} = \sqrt{\frac{0.07 \cdot 0.93}{200}} = \underline{0.018}$$

b) ① SRS ? assume

② $np \geq 10$ ✓
 $nq \geq 10$ ✓

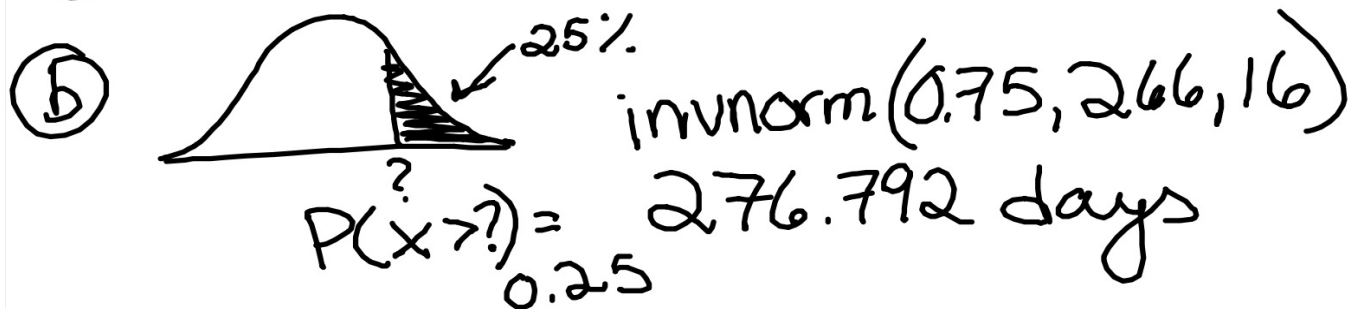
③ $pop \geq 10n$ ✓

$$N(0.07, 0.018)$$

c) $P(\hat{p} > 0.10)$

③⑦ $N(266, 16)$

② $P(270 < X < 280) = 0.211$



③ $n = 60$

① SRS ? assume $N(266, \frac{16}{\sqrt{60}})$

② norm pop ✓

or
 $n \geq 30$

③ pop $\geq 10n$ ✓

$$④ P(\bar{X} < 260)$$

$$\text{normcdf}(-E99, 260, 266, \frac{16}{\sqrt{60}})$$

$$0.0018$$

Book problems:

p. 434 #16, 20, 22, 38, 48

\hat{p} \bar{x}

① write model & important info
 $N(_, _)$

② check conditions/assumptions
state & check

$$n_p \geq 10 \quad 100 \checkmark$$

$$n_g \geq 10 \quad 55 \checkmark$$

16) $p = 0.30$ $n = 100$

- (a) (1) SRS stated
(2) $np \geq 10$ $30 \geq 10$
 $nq \geq 10$ $70 \geq 10$
(3) $pop \geq 10n$ over 1000 people wear contacts

$N(0.30, 0.0458)$

(b) $P(p > 1/3) = \text{normcdf}(0.3333, E99, 0.30, 0.0458) = 0.2336$

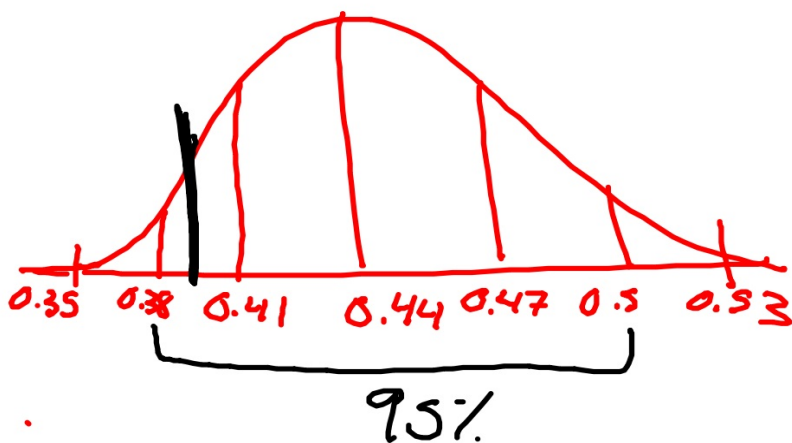
20) $p = 0.44$ $n=244$

$N(0.44, 0.03)$

- (1) SRS assumed
 $np \geq 10$ 107.36 $\neq 10$
 $nq \geq 10$ 136.64 $\neq 10$
 $pop > 10n$ there are more than 2440 binge drinkers

$$\hat{p} = \frac{96}{244} = 39.3\%$$

$$N(0.44, 0.03)$$



22 $p = 0.92$
 $n = 160$

① SRS assumed

$$\begin{array}{l} np \geq 10 \quad 147.2 \checkmark \\ nq \geq 10 \quad 12.8 \checkmark \end{array}$$

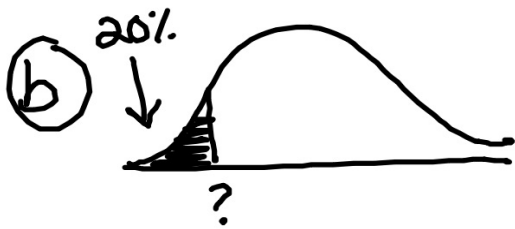
pop ≥ 10 more than 1600 seeds \checkmark

$$N(0.92, 0.0214)$$

$$P(\hat{p} > 0.95) = 0.0805$$

38) a) $N(35.4, 4.2)$

$$P(X > 40) = 0.1367$$



$$P(X < ?) = 0.20$$

$$\text{invnorm}(0.20, 35.4, 4.2)$$

$$= 31.87''$$

③ $n = 4$

① SRS assumed

② norm pop or $n \geq 30$ normal pop. stated

③ pop $\geq 10n$ more than 40 yrs w/ rain ✓

$$N(35.4, \frac{4.2}{\sqrt{4}}) \Rightarrow N(35.4, 2.1)$$

d) $P(\bar{X} < 30) = 0.0051$

48) $N(10.2, 0.12)$

a) $P(X < 10) = 0.0478$

c) $n = 3$

① SRS ✓

② norm pop ✓

③ pop ≥ 10 more than 30 bags ✓

$N(10.2, \frac{0.12}{\sqrt{3}})$

$P(\bar{X} < 10) = 0.0019$

$$\textcircled{a} P(\bar{X} < 10)$$

$$N(10.2, \frac{0.12}{\sqrt{24}})$$

$$\textcircled{b} P = 0.05 \leftarrow \text{under}$$

$$\underline{0.95} - \underline{0.95} - \underline{0.95}$$